

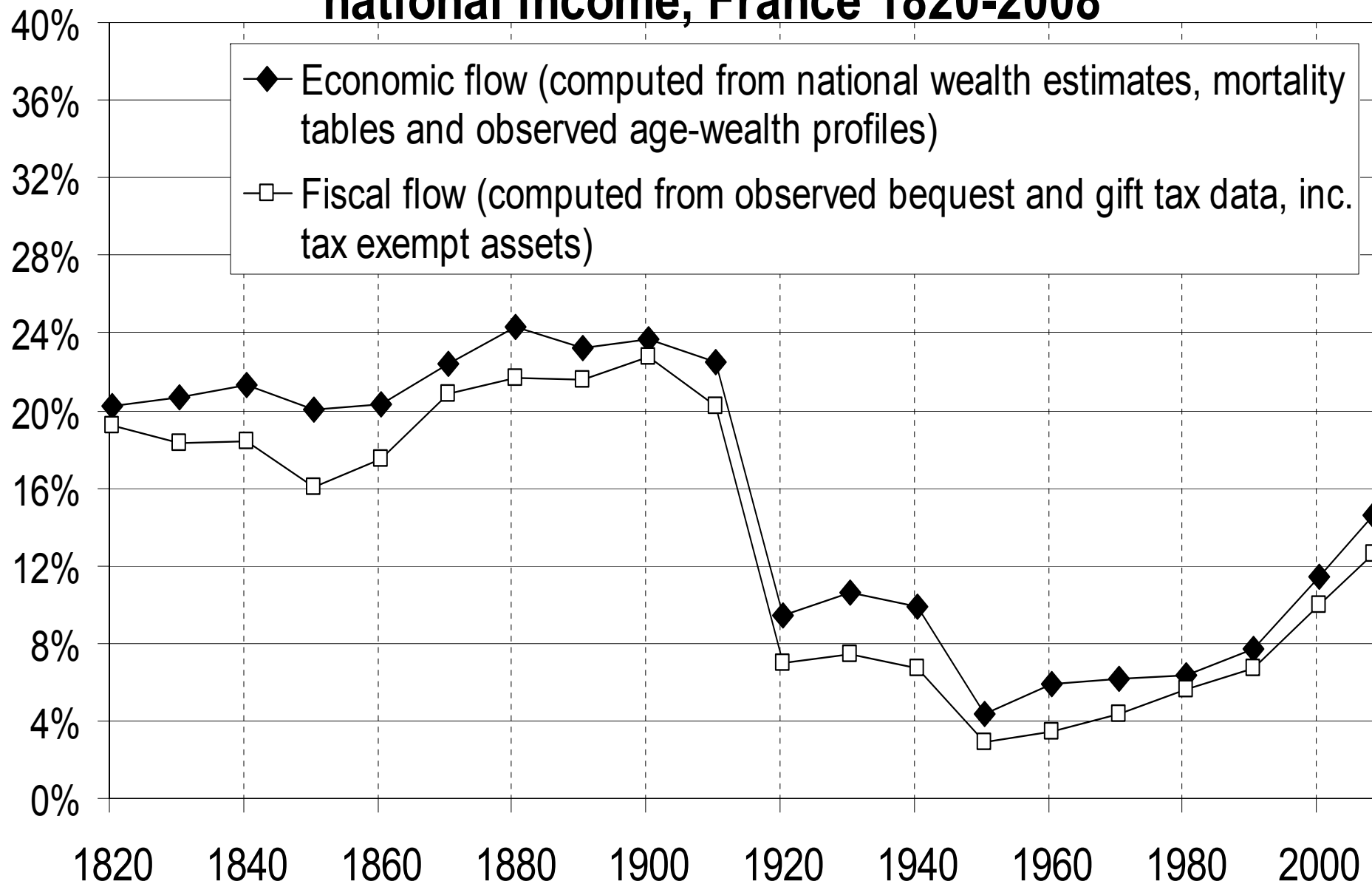
**On the Long-run  
Evolution of Inheritance  
France 1820-2050**

Thomas Piketty  
Paris School of Economics  
September 2010

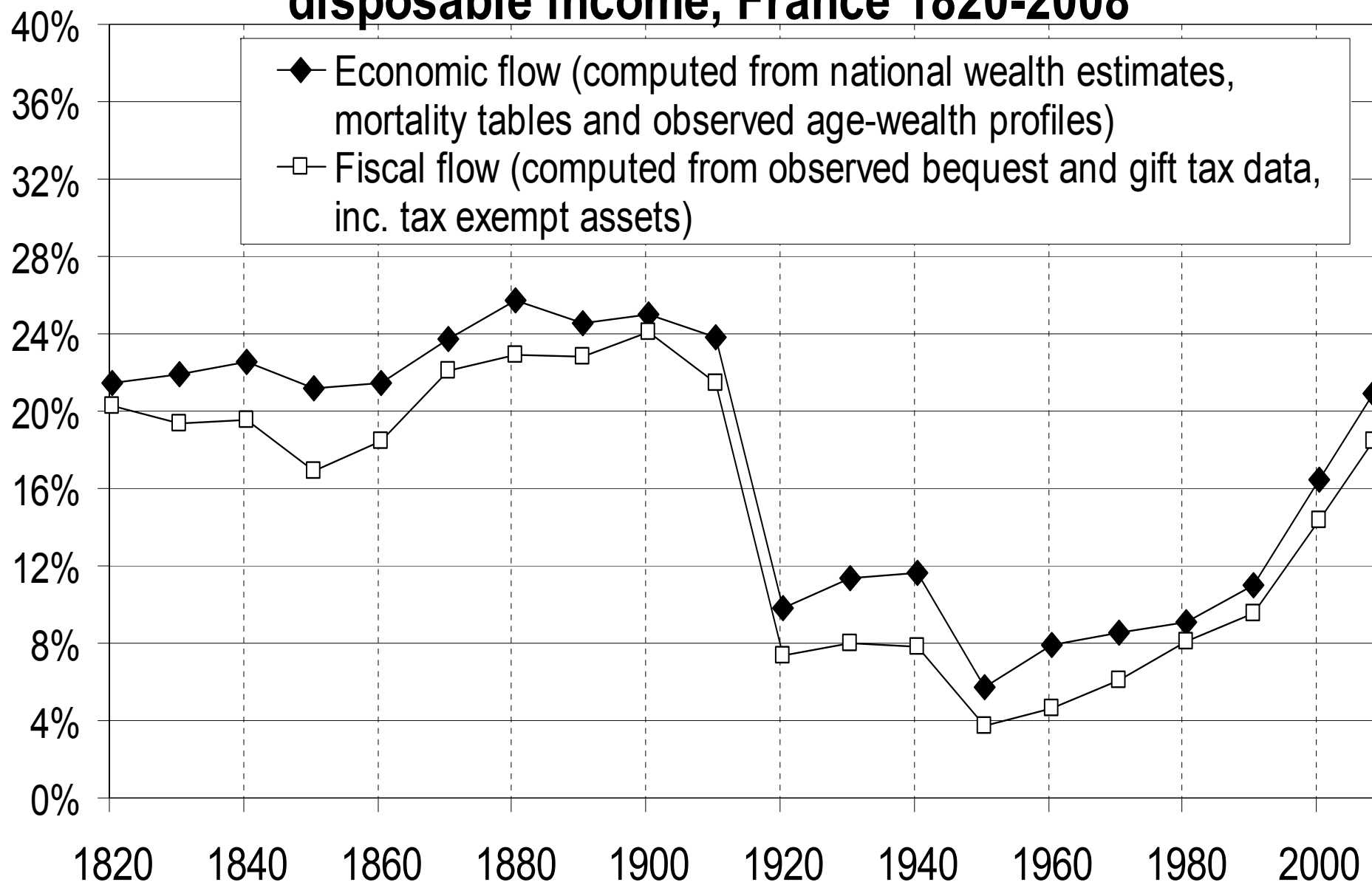
- **There are two ways to become rich:** either through one's own work, or through inheritance
- In the 19th century and early 20th, it was obvious to everybody that the 2nd channel was important: inheritance and successors are everywhere in the literature; huge inheritance flow in tax data

- **Q:** Does this belong to the past? Did modern growth kill the inheritance channel? E.g. rise of human capital and meritocracy?
- This paper answers « **NO** » to this question and attempts to explain why, taking France 1820-2050 as an illustration

**Figure 1: Annual inheritance flow as a fraction of national income, France 1820-2008**



**Figure 2: Annual inheritance flow as a fraction of disposable income, France 1820-2008**



# What this paper does

- Documents & explains this fact; draws lessons for other countries
- **Main lesson: with  $r > g$  (say,  $r = 4\% - 5\%$  vs  $g = 1\% - 2\%$ ), then wealth coming from the past is being capitalized faster than growth, & inherited wealth dominates self-made wealth**
- Dynastic model: heirs save a fraction  $g/r$  of the return to inherited wealth, so that wealth-income ratio  $\beta = W/Y$  is stationary. Then steady-state bequest flow  $b_y = B/Y = \beta/H$ , with  $H =$  generation length. If  $\beta = 600\%$ ,  $H = 30 \rightarrow b_y = 20\%$
- This can be generalized to more general saving models: if  $g$  small &  $r > g$ , then  $b_y$  close to  $\beta/H$

# Application to the structure of lifetime inequality

- Top incomes literature: Atkinson-Piketty OUP 2007 & 2010 → 23 countries.. but pb with capital side: we were not able to decompose labor-based vs inheritance-based inequality, i.e. meritocratic vs rentier societies
- **This paper = positive aggregate analysis; but building block for future work with heterogeneity, inequality & optimal taxation**

# Data sources

- **Estate tax data:** aggregate data 1826-1964; tabulations by estate & age brackets 1902-1964; national micro-files 1977-1984-1987-1994-2000-2006; Paris micro-files 1807-1932
- **National wealth and income accounts:** Insee official series 1949-2009; linked up with various series 1820-1949



- **French estate tax data is exceptionally good:** universal, fully integrated bequest and gift tax since 1791
- Key feature: everybody has to fill a return, even with very low estates
- 350,000 estate tax returns/year in 1900s and 2000s, i.e. 65% of the 500,000 decedents (*US: < 2%*)

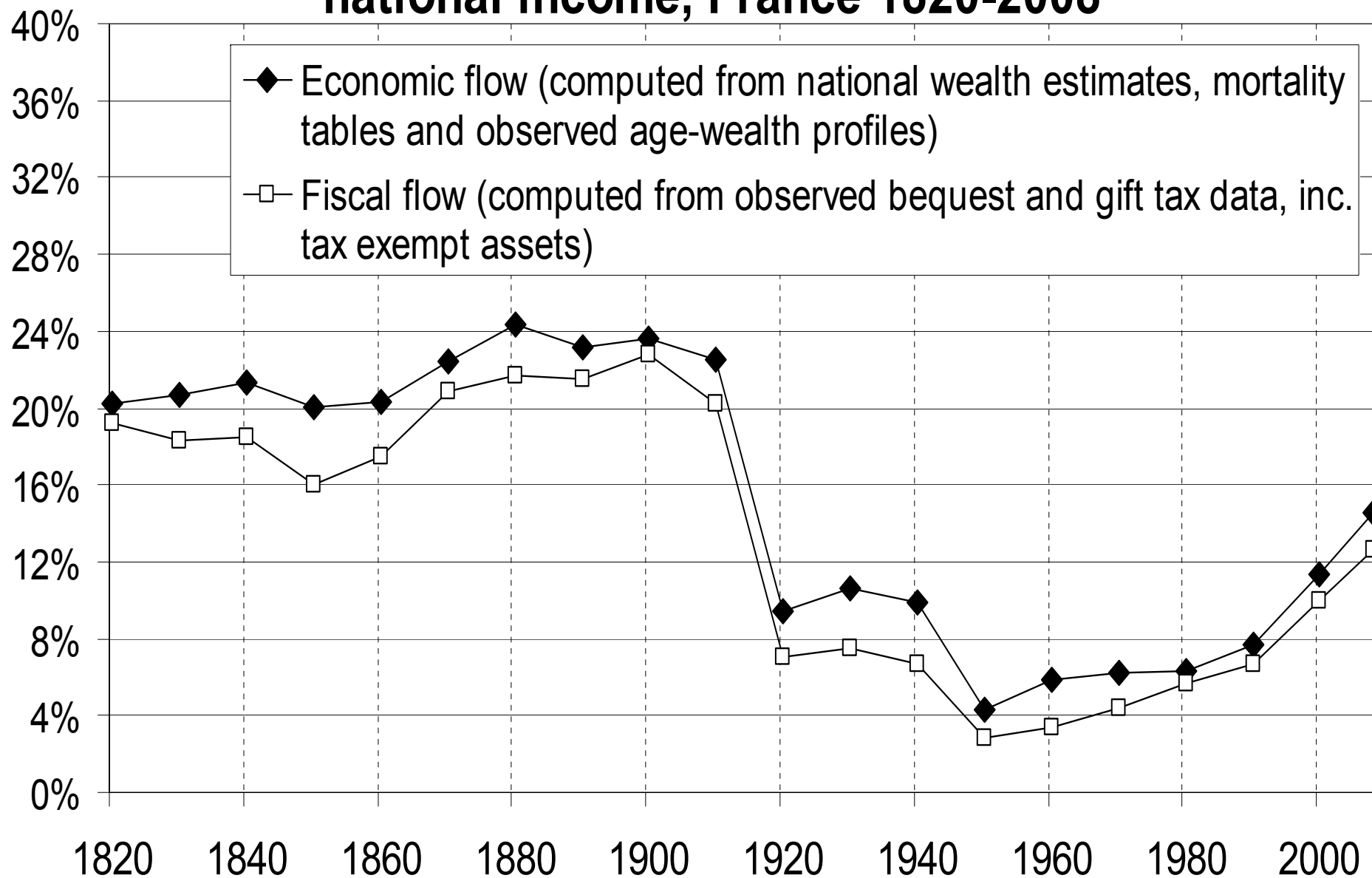
*(memo: bottom 50% wealth share < 10%)*

# Computing inheritance flow

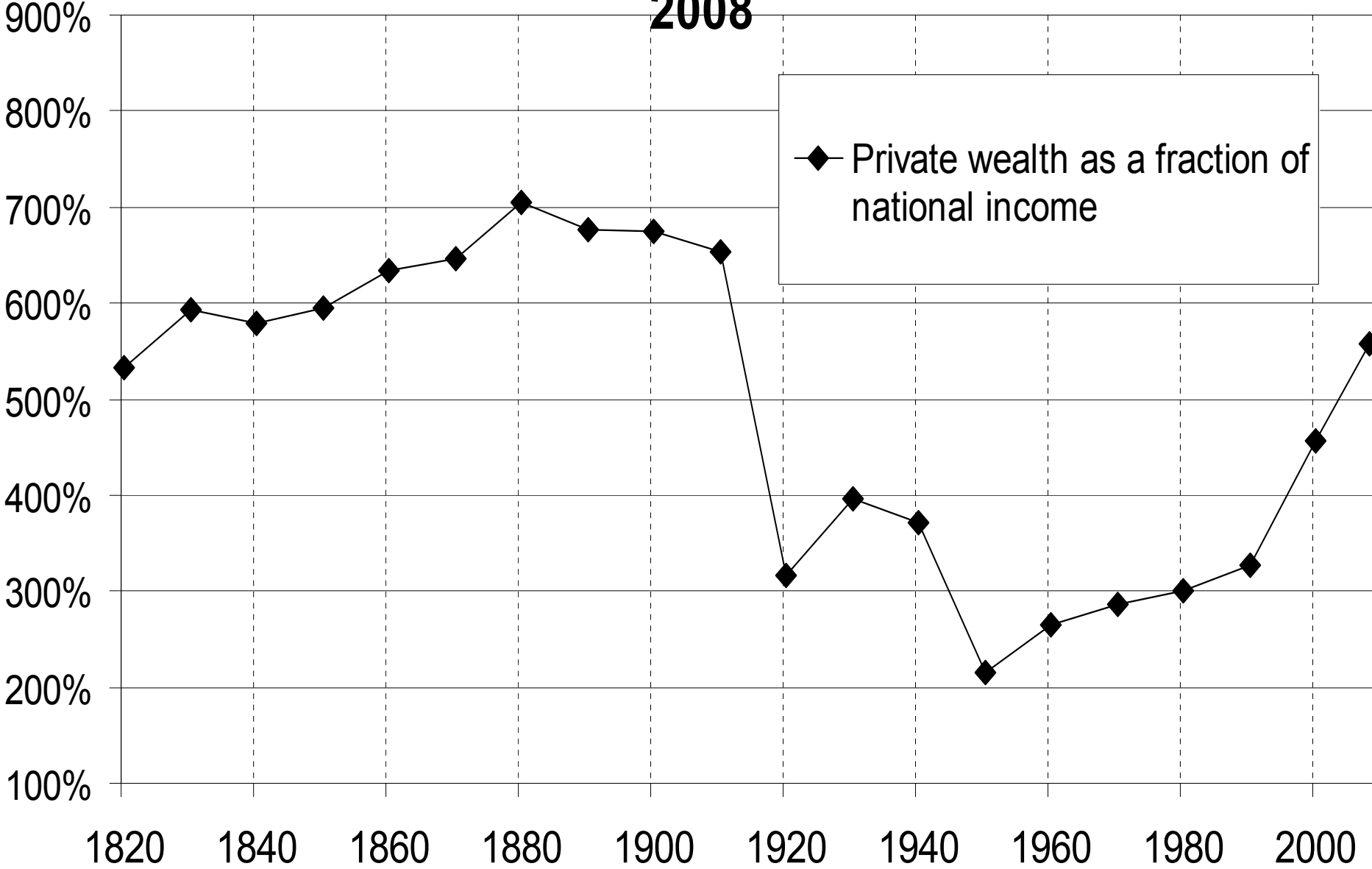
$$\mathbf{B}_t/Y_t = \mu_t \ m_t \ \mathbf{W}_t/Y_t$$

- $W_t/Y_t$  = aggregate wealth/income ratio
  - $m_t$  = aggregate mortality rate
  - $\mu_t$  = ratio between average wealth of decedents and average wealth of the living (= age-wealth profile)
- The U-shaped pattern of inheritance is the product of three U-shaped effects

# Figure 1: Annual inheritance flow as a fraction of national income, France 1820-2008

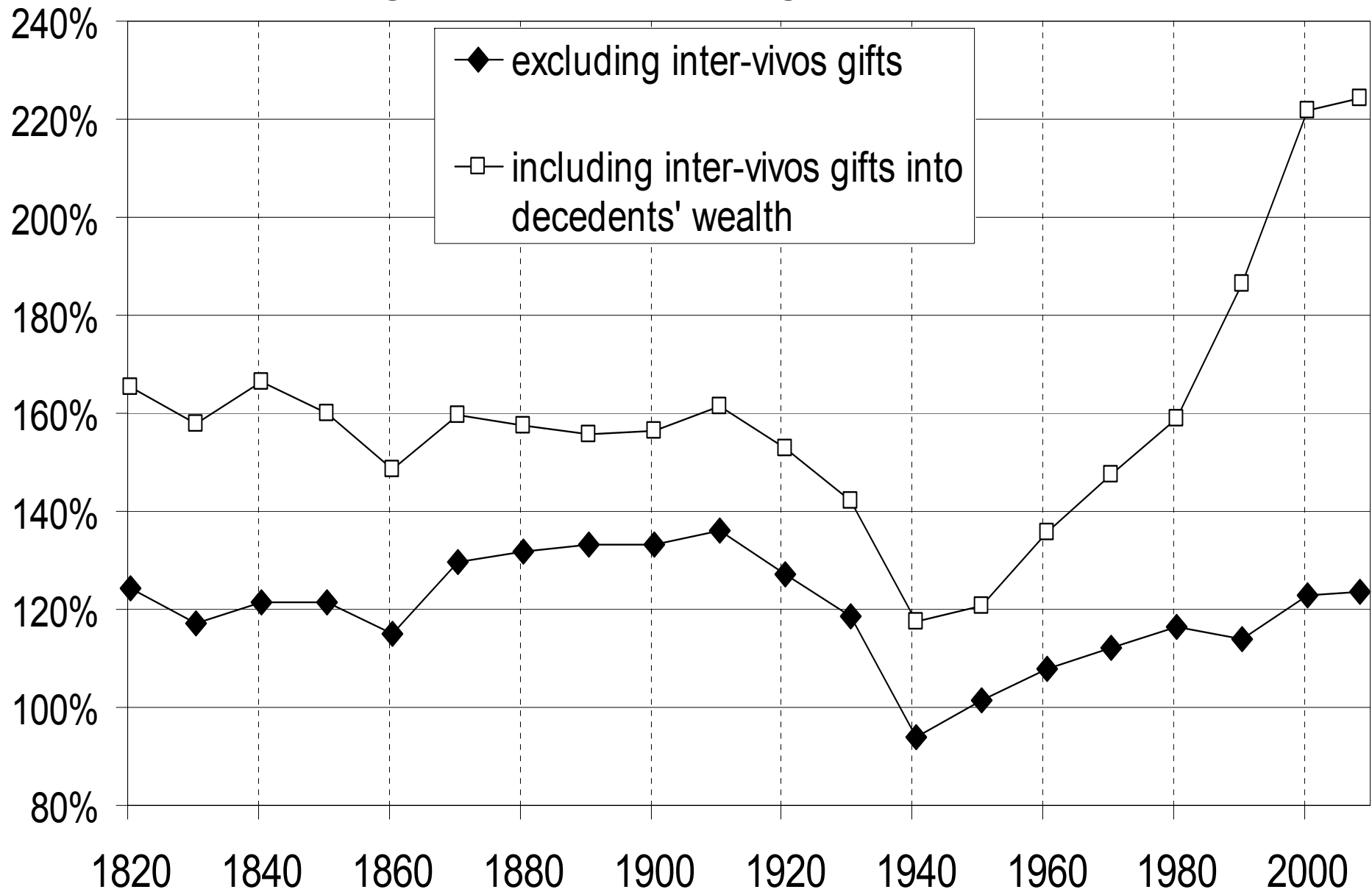


**Figure 4: Wealth/income ratio in France 1820-  
2008**



- 1900s:  $Y = 35$  billions francs or,  $W = 250$  billions,  $B = 8.5$  billions  
→  $W/Y = 700\%$ ,  $B/Y = 25\%$
- 2008:  $Y = 1\,700$  billions € (i.e. 35 000€ per adult),  $W = 9\,500$  billions € (200 000€ per adult),  $B = 240$  billions €  
→  $W/Y = 560\%$ ,  $B/Y = 15\%$
- Between 1900s and 1950s,  $W/Y$  divided by 3, but  $B/Y$  divided by 6 → the fall in  $W/Y$  explains about half of the fall in  $B/Y$

**Figure 8: The ratio between average wealth of decedents and average wealth of the living in France 1820-2008**



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**Table 2: Raw age-wealth-at-death profiles in France, 1820-2008**

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	<b>20-29</b>	<b>30-39</b>	<b>40-49</b>	<b>50-59</b>	<b>60-69</b>	<b>70-79</b>	<b>80+</b>
<b>1827</b>	50%	63%	73%	<b>100%</b>	113%	114%	122%
<b>1857</b>	57%	58%	86%	<b>100%</b>	141%	125%	154%
<b>1887</b>	45%	33%	63%	<b>100%</b>	152%	213%	225%
<b>1902</b>	26%	57%	78%	<b>100%</b>	172%	176%	233%
<b>1912</b>	23%	54%	74%	<b>100%</b>	158%	176%	237%
<b>1931</b>	22%	59%	77%	<b>100%</b>	123%	137%	143%
<b>1947</b>	23%	52%	77%	<b>100%</b>	99%	76%	62%
<b>1960</b>	28%	52%	74%	<b>100%</b>	110%	101%	87%
<b>1984</b>	19%	55%	83%	<b>100%</b>	118%	113%	105%
<b>2000</b>	19%	46%	66%	<b>100%</b>	122%	121%	118%
<b>2006</b>	25%	42%	74%	<b>100%</b>	111%	106%	134%

# How can we account for these facts?

- 1914-45 capital shocks played a big role, and it took a long time to recover
- Key question: why does the age-wealth profile become upward-sloping again?

→ **the  $r > g$  effect**

- **Where does the  $B/Y=20\%-25\%$  magic number come from? Why  $\mu_t \uparrow$  seem to compensate exactly  $m_t \downarrow$ ?**



# Theory 1: Demography

- To simplify: deterministic, stationary demographic structure: everybody becomes adult at age  $A$ , has one kid at age  $H$ , inherits at age  $I$ , and dies at age  $D$
- 1900:  $A=20$ ,  $H=30$ ,  $D=60 \rightarrow I=D-H=30$
- 2050:  $A=20$ ,  $H=30$ ,  $D=80 \rightarrow I=D-H=50$
- mortality rate among adults:

$$m_t = 1/(D-A)$$

(1900: about 2.5%; 2050: about 1.7%)

# Theory 2: Production

- $Y_t = F(K_t, H_t) = F(K_t, e^{gt} L_t)$
- $g$  = exogenous productivity growth rate
- E.g. Cobb-Douglas:  $F(K, H) = K^\alpha H^{1-\alpha}$
- $Y_t = Y_{K_t} + Y_{L_t}$ , with  $Y_{K_t} = r_t K_t = \alpha_t Y_t$
- Define  $\beta_t = K_t/Y_t = W_t/Y_t$  (closed economy)  
(*open economy:  $W_t = K_t + FW_t$  (+ $D_t$ )*)
- Then  $\alpha_t = r_t \beta_t$ , i.e.  $r_t = \alpha_t/\beta_t$
- E.g. if  $\beta_t = 600\%$ ,  $\alpha_t = 30\%$ , then  $r_t = 5\%$

# Theory 3: Savings

- Aggregate savings rate = stable at about 10% of  $Y_t$  since 1820
- $\beta^* = s/g$  ( $g=1\%$  &  $s=6\%$  →  $\beta^* = 600\%$ )
- Exogenous saving:  $S_t = sY_t = s_L Y_{Lt} + s_K rW_t$
- **Is  $s_K > s_L$ ?**
- **Dynastic utility function:  $s_K = g/r$ ,  $s_L = 0$**
- **Bequest in the utility function:  $U(C, B)$**
- easy to generate  $s_K > s_L$  (or  $s_K < s_L \dots$ )

- **Dynastic model:**  $U = \int e^{-\theta t} C_t^{1-\sigma}/(1-\sigma)$

→ Ramsey steady-state:

$$r^* = \theta + \sigma g \quad (> g)$$

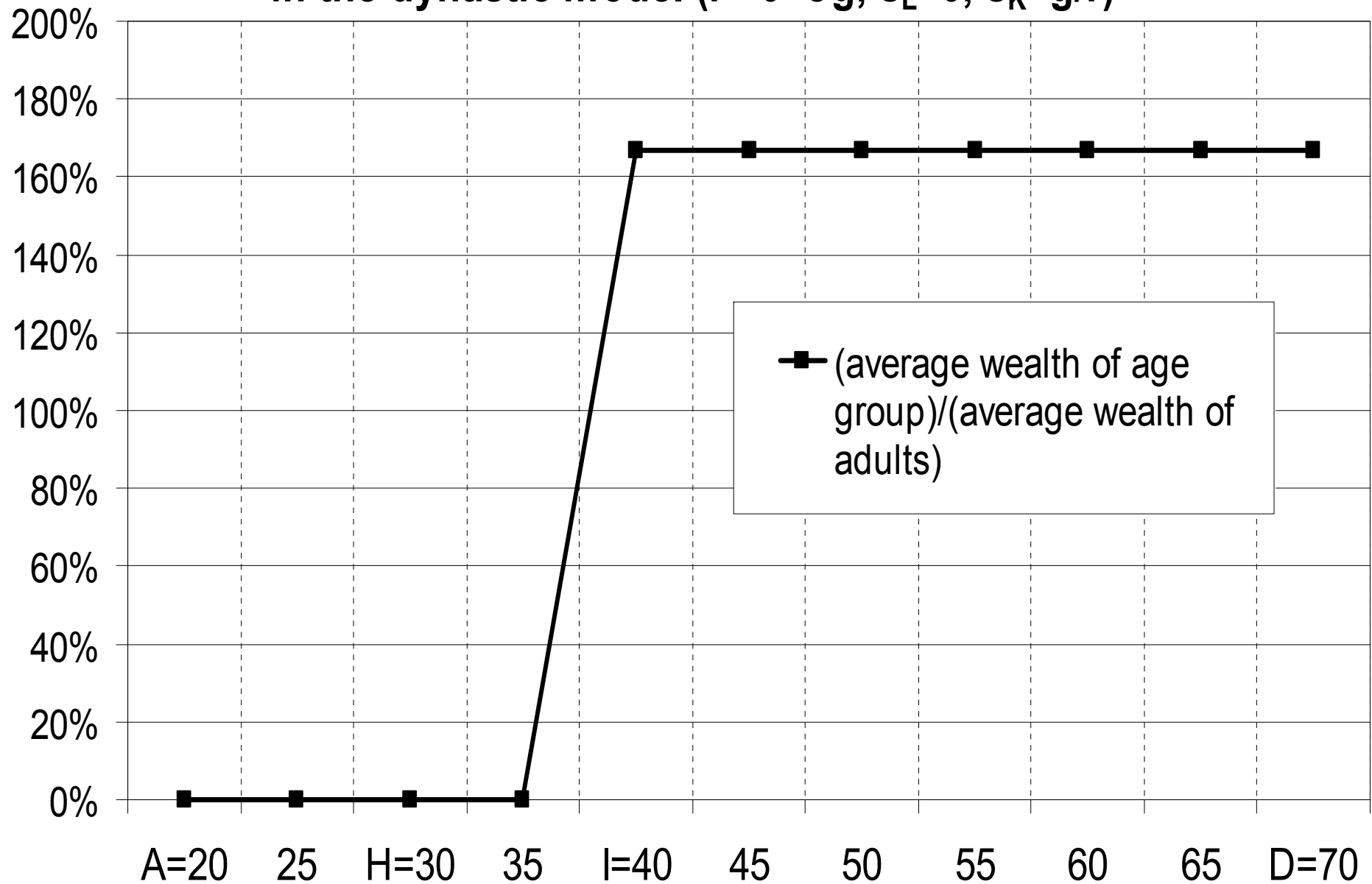
- In effect:  $s_L^* = 0\%$ ,  $s_K = g/r^*\%$
- Any wealth distribution s.t.  $f'(k^*) = r^*$  is a steady-state
- Intuition:  $Y_{L_t}$  grows at rate  $g$ , workers don't need to save; but capitalists need to save a fraction  $g/r$  of their capital income  $Y_{K_t} = r W_t$ , so that  $W_t$  grows at rate  $g$

# Steady-state age-wealth profile

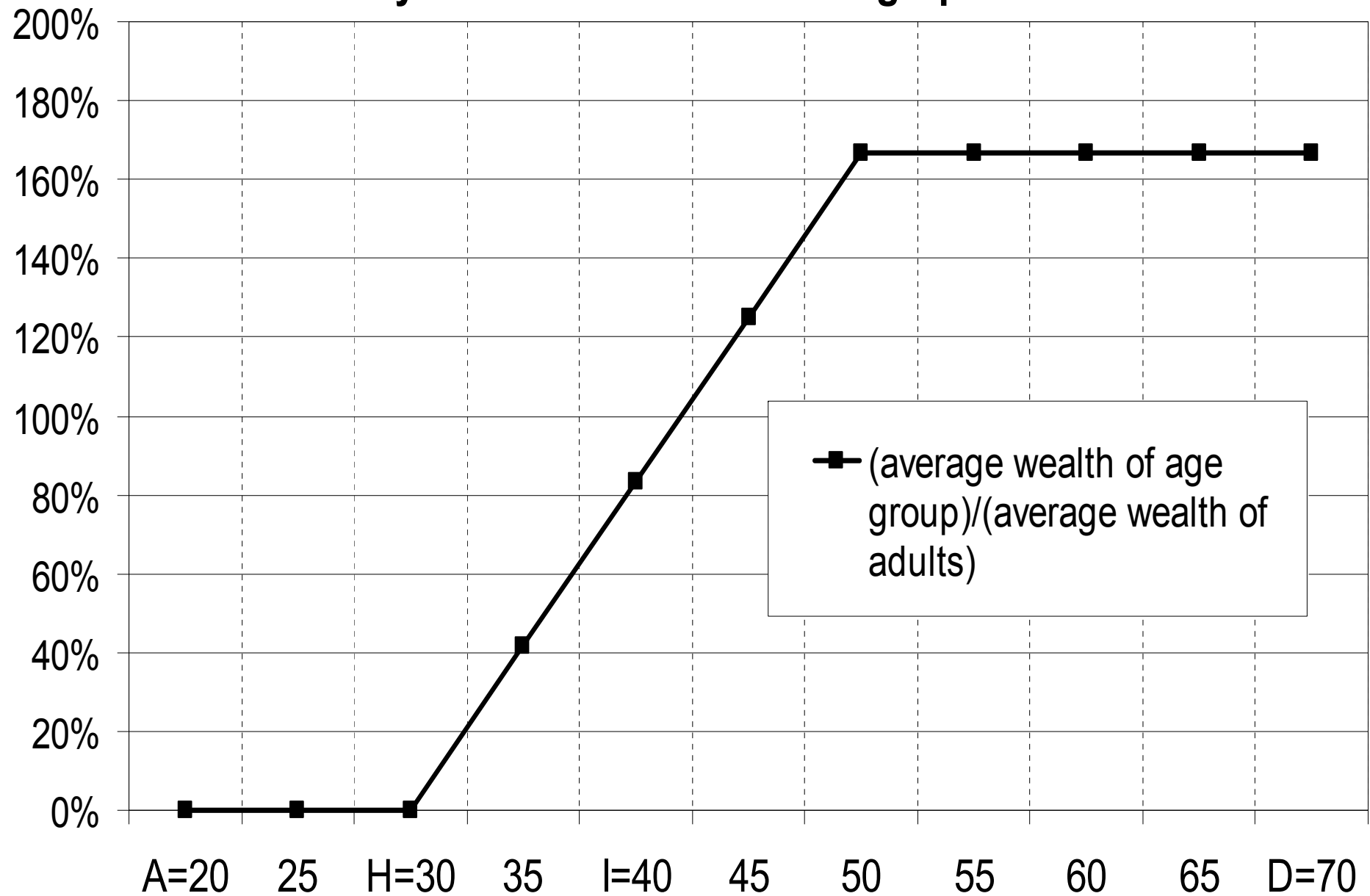
- If  $s_L = 0\%$ , then the cross-sectional age-wealth profile  $W_t(a)$  at time  $t$  is very simple:
  - If  $A < a < I$ , then  $W_t(a) = 0$  (zero wealth until age of inheritance)
  - If  $I < a < D$ , then  $W_t(a) = W_t^{\text{old}}$  (growing at rate  $g$ , but independent of age  $a$ )

Intuition: young heirs receive larger estate (growing at rate  $g$ ), but older heirs have capitalized their estate at rate  $s_K = g/r$ , so that the cross-sectional profile is flat

**Figure 9: Steady-state cross-sectional age-wealth profile  
in the dynastic model ( $r = \theta + \sigma g$ ,  $s_L = 0$ ,  $s_K = g/r$ )**



**Figure 10: Steady-state cross-sectional age-wealth profile  
in the dynastic model with demographic noise**



**Proposition 1:** Steady-state of dynastic model :

$$r = \theta + \sigma g (> g), s_L = 0, s_K = g/r, \mu = (D - A)/H (> 1)$$

→ **B/Y is independent of life expectancy:**

$$\mu = (D - A)/H, m = 1/(D - A), \text{ so}$$

$$\mathbf{B/Y = \mu m W/Y = \beta/H}$$

E.g. if  $\beta = 600\%$ ,  $H = 30$ , then **B/Y = 20%**

1900:  $D = 60$ ,  $I = 30$ ,  $m = 2.5\%$ , but  $\mu = 133\%$

2050:  $D = 80$ ,  $I = 50$ ,  $m = 1.6\%$ , but  $\mu = 200\% \gg$

**Proposition 2:** More generally:

$$\mu = [1 - e^{-(g - s_K r)(D - A)}] / [1 - e^{-(g - s_K r)(D - I)}]$$

→  $\mu'(s_K) > 0$ ,  $\mu'(r) > 0$ ,  $\mu'(g) < 0$

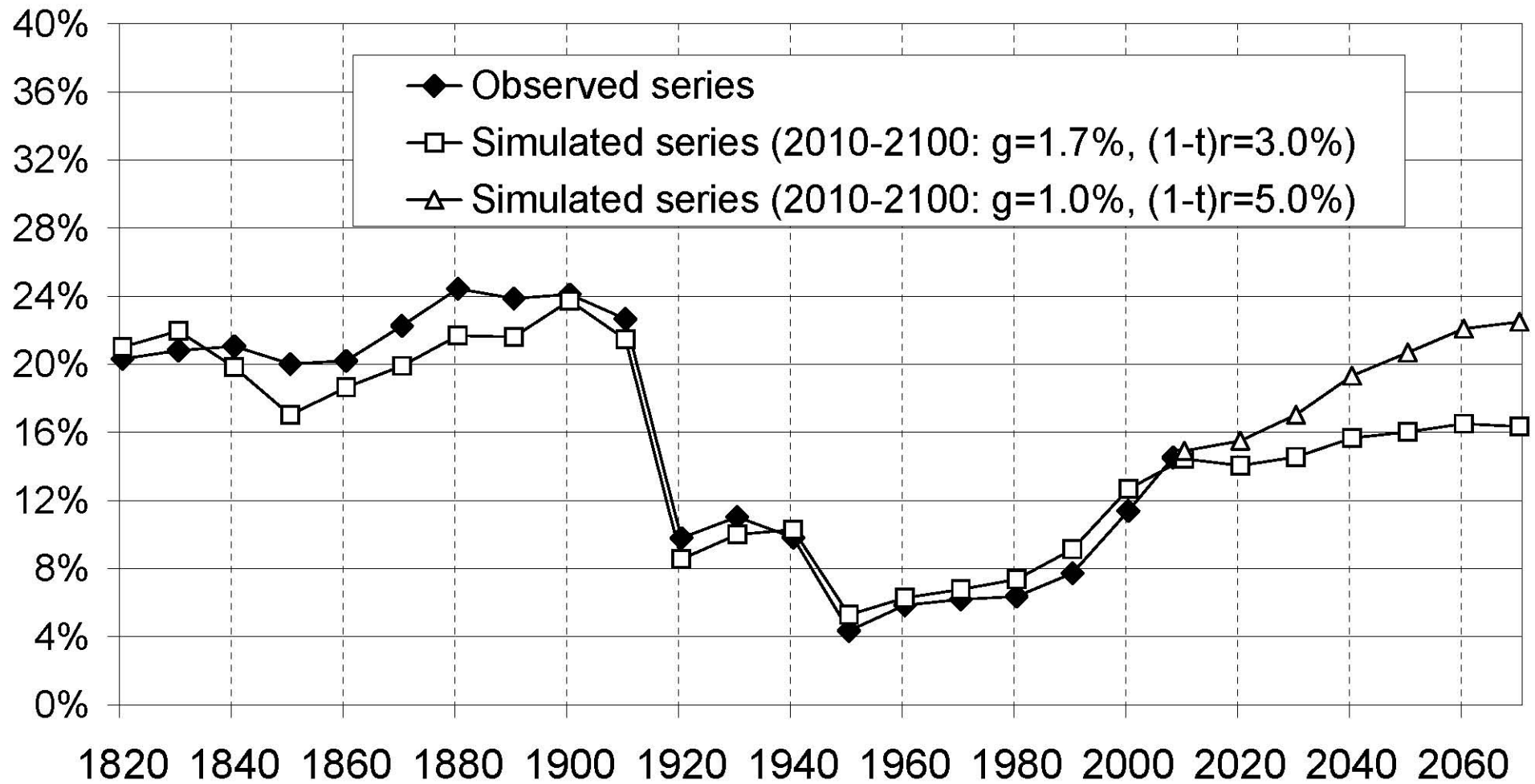
(→ **for  $g$  small,  $\mu$  close to  $(D - A)/H$ )**



# Simulations

- I start from the observed age-wealth profile  $W_t(a)$  in 1820 or 1900
- I take  $s_t$  and  $r_t$  from national accounts
- I take observed age-labor income (+transfer income) profiles
- I apply observed mortality rates by age group, and observed age structure of heirs, donors and donees
- I try different savings behavior to replicate observed dynamics of  $\mu_t$  &  $B_t/Y_t$

**Figure 9: Observed vs simulated inheritance flow B/Y, France 1820-2100**



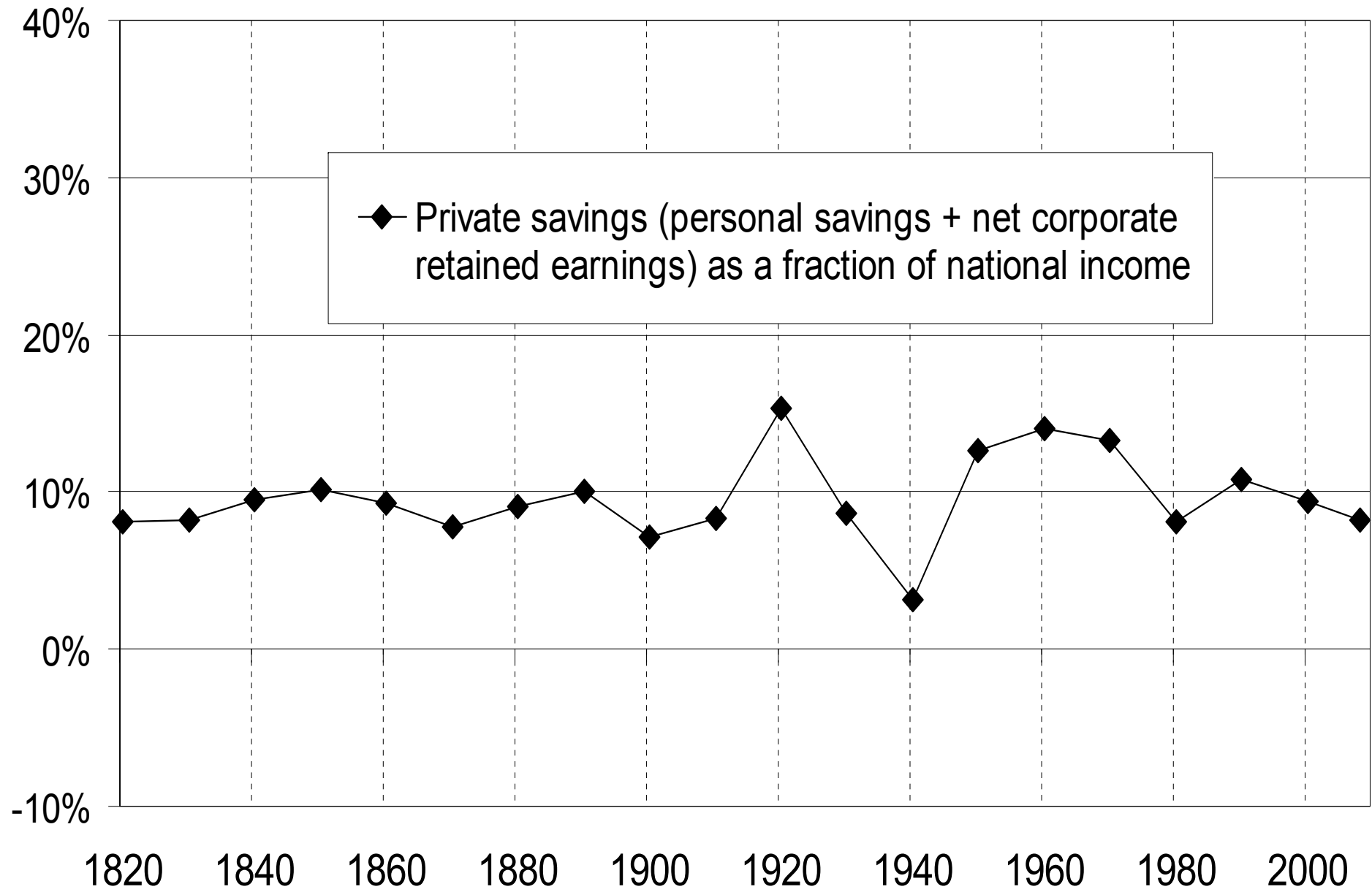
# Simulations 1: 19th century

- France 1820-1910 = quasi-steady-state
- $\beta = W/Y = 629\%$ ,  $g=1.0\%$ ,  $s=10.1\%$ ,  
 $\alpha=38\% \rightarrow r = 6.0\% \gg g=1.0\%$
- **Key fact about 19th century growth = rate of return  $r$  much bigger than  $g$**   
 **$\rightarrow$  wealth holders only need to save a small fraction of their capital income to maintain a constant or rising  $W/Y$**   
(  $g_w = s/\beta = 1.3\% \rightarrow W/Y$  was slightly rising)

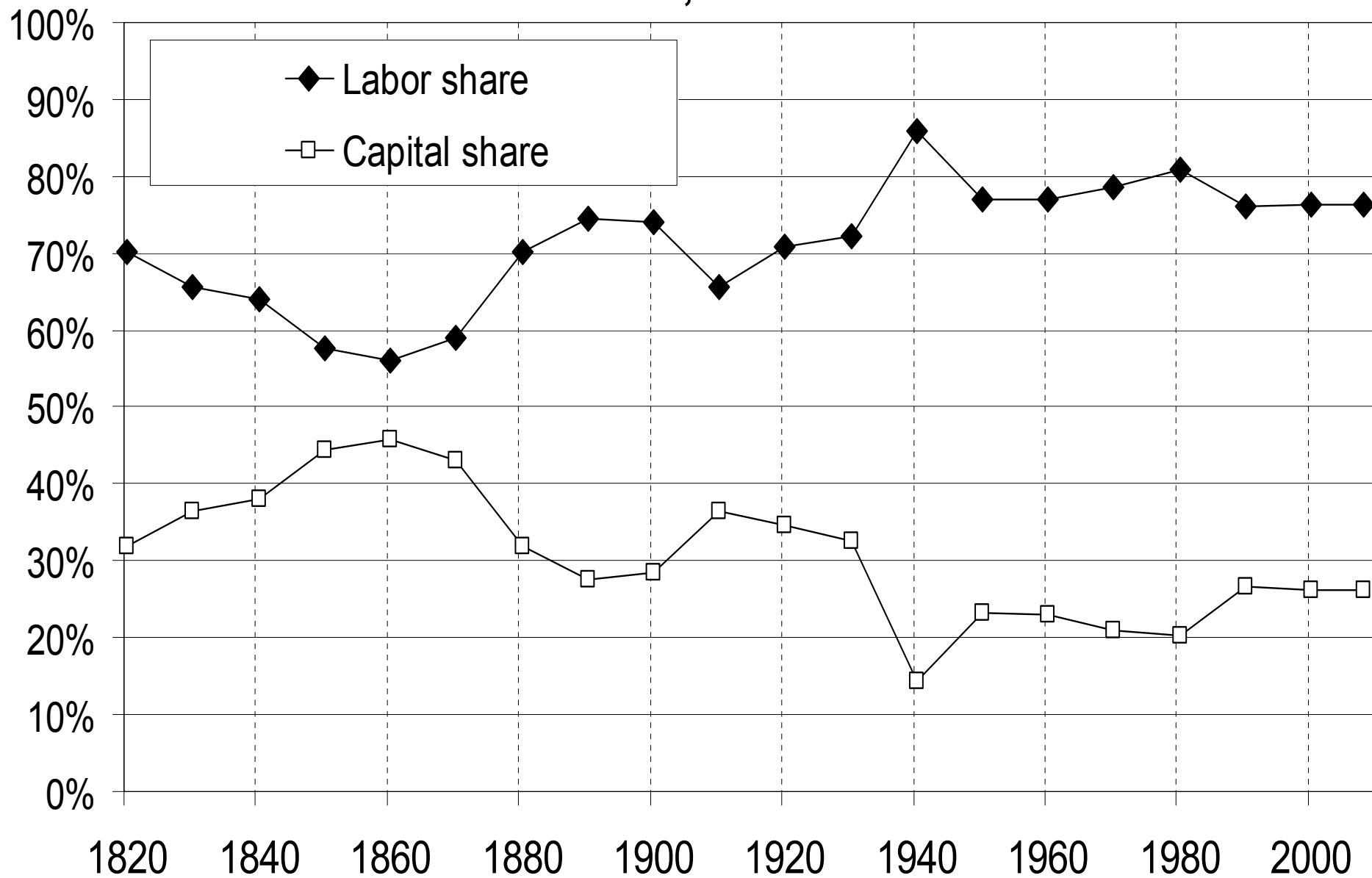
→ in order to reproduce both the 1820-1910 pattern of  $B/Y$  **and** the observed age-wealth profile (rising at high ages), one needs to assume that most of the savings came from capital income (i.e.  $s_L$  close to 0 and  $s_K$  close to  $g/r$ )

(consistent with high wealth concentration of the time)

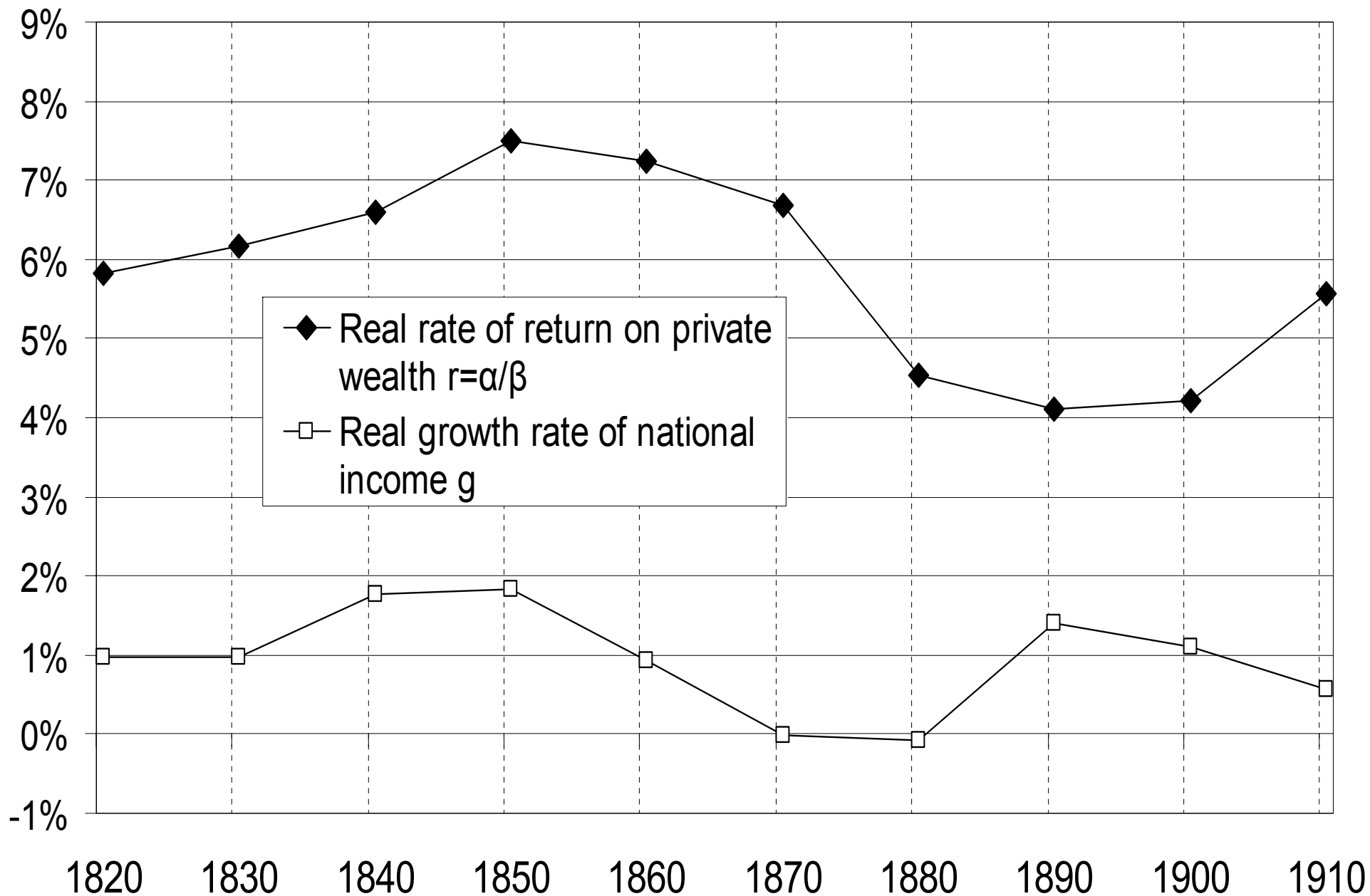
**Figure 11: Private savings rate in France 1820-2008**



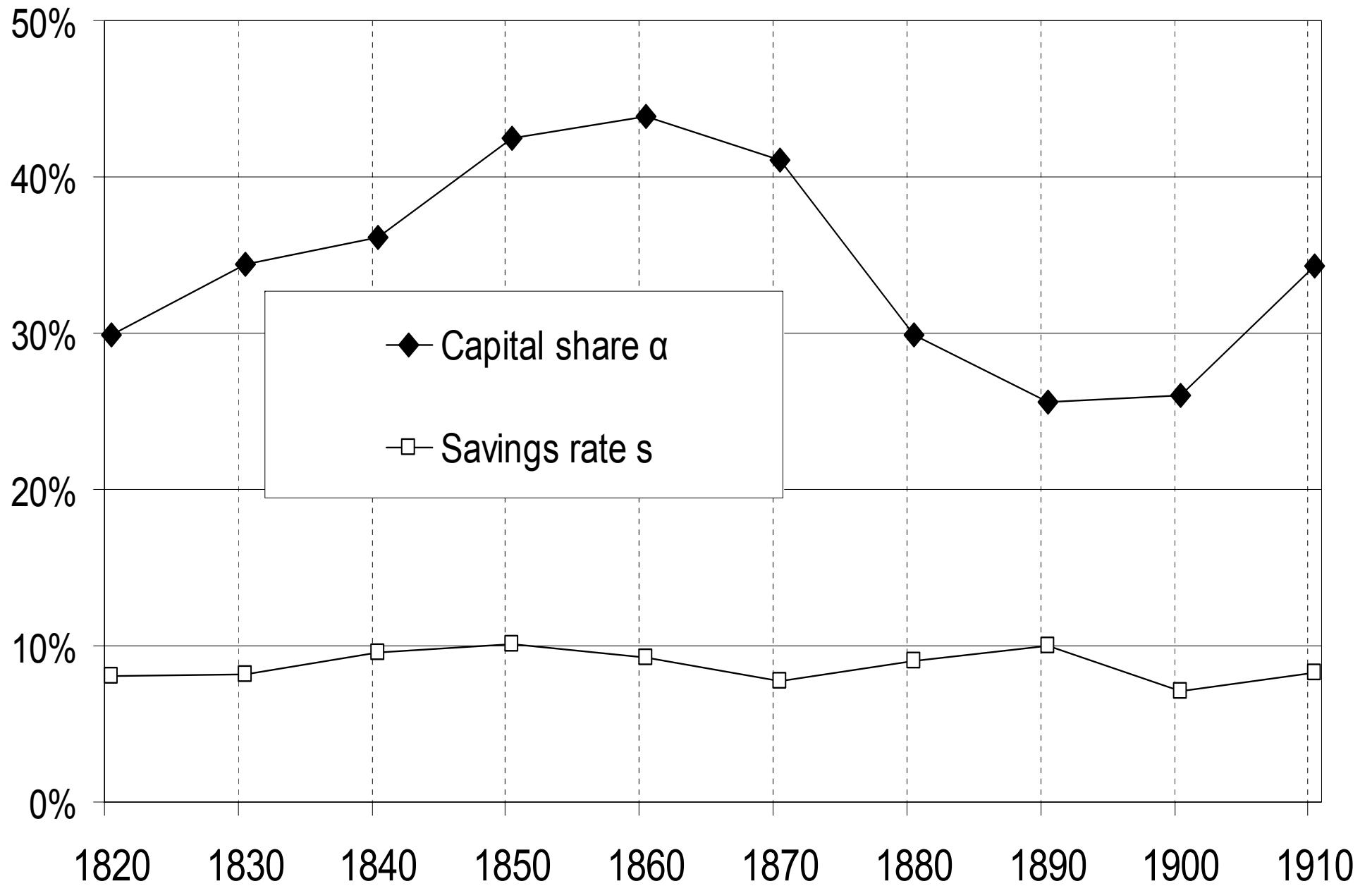
**Figure 13: Labor & capital shares in (factor-price) national income, France 1820-2008**



**Figure 14: Rate of return vs growth rate France 1820-1913**



**Figure 15: Capital share vs savings rate France 1820-1913**





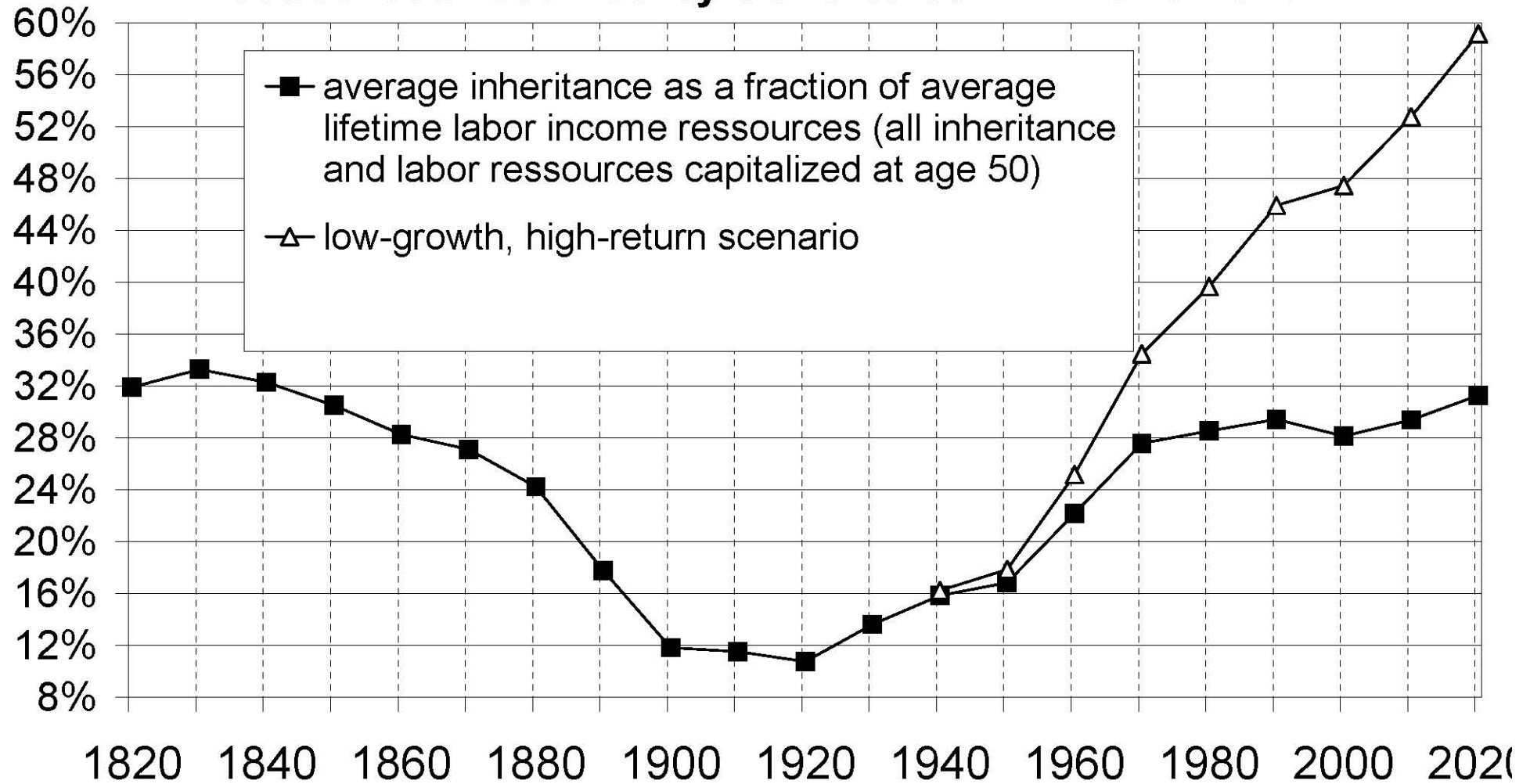
# Simulations 2: 20th & 21st centuries

- Uniform savings  $s=s_K=s_L$  can reproduce both B/Y & observed age-wealth profiles over 1900-2008
- **2010-2050 simulations:**  $g=1.7\%$ ,  $s=9.4\%$ ,  $\alpha=26\%$ , after-tax  $r=3.0\%$   
→ B/Y stabilizes at 16%
- But if  $g=1.0\%$  & after-tax  $r=4.5\%$  (rising global k share and/or k tax cuts), then B/Y converges towards 22%-23%

# **Applications to distributional analysis**

- **19<sup>c</sup>: top successors dominate top labor earners; top 1% spouse > top 1% job**
- **Cohorts born in 1900s-1950s: for the first time maybe in history, top labor incomes dominate top successors**
- **Cohorts born in 1970s-1980s & after: closer to 19<sup>c</sup> rentier society than to 20<sup>c</sup> meritocratic society. E.g. with labor income alone, hard to buy an apartment in Paris..**

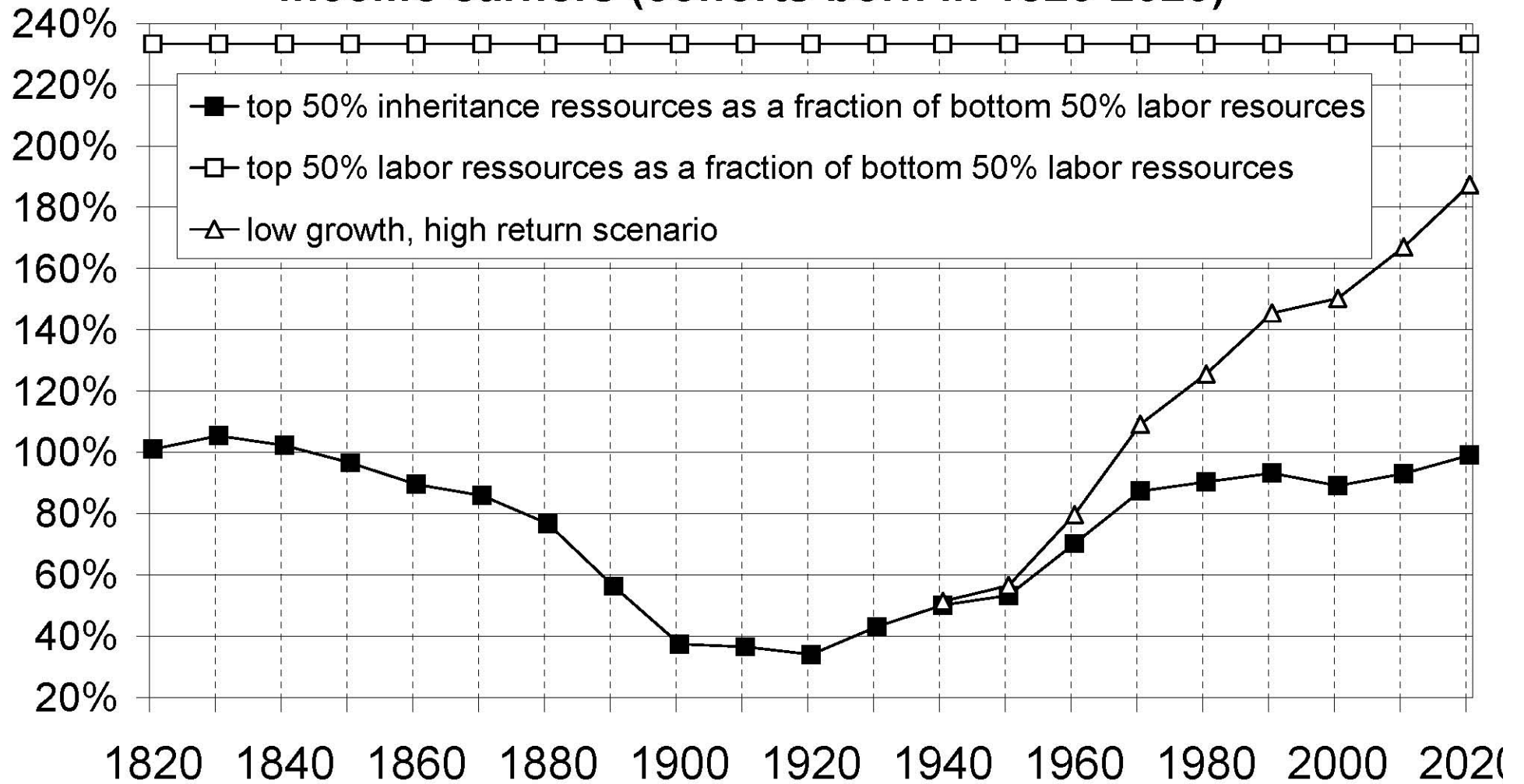
**Figure 11: The share of inheritance in lifetime resources received by cohorts born in 1820-2020**



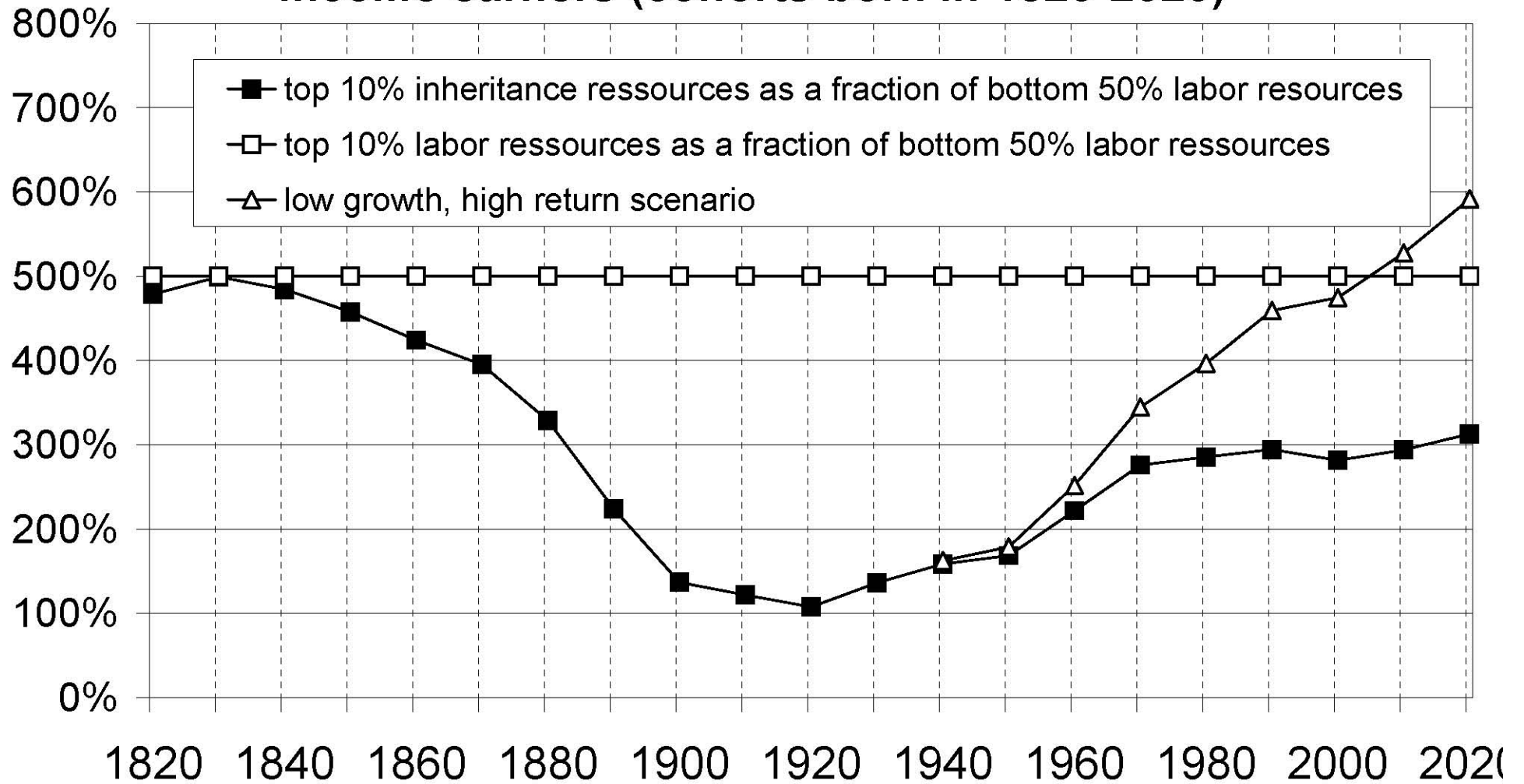
**Table 3: Intra-cohort distributions of labor income and inheritance, France, 1910 vs 2010**

Shares in aggregate labor income or inherited wealth	Labor income 1910-2010	Inherited wealth	
		1910	2010
<b>Top 10% "Upper Class"</b>	<b>30%</b>	<b>90%</b>	<b>60%</b>
<i>incl. Top 1% "Very Rich"</i>	<i>6%</i>	<i>50%</i>	<i>25%</i>
<i>incl. Other 9% "Rich"</i>	<i>24%</i>	<i>40%</i>	<i>35%</i>
<b>Middle 40% "Middle Class"</b>	<b>40%</b>	<b>5%</b>	<b>35%</b>
<b>Bottom 50% "Poor"</b>	<b>30%</b>	<b>5%</b>	<b>5%</b>

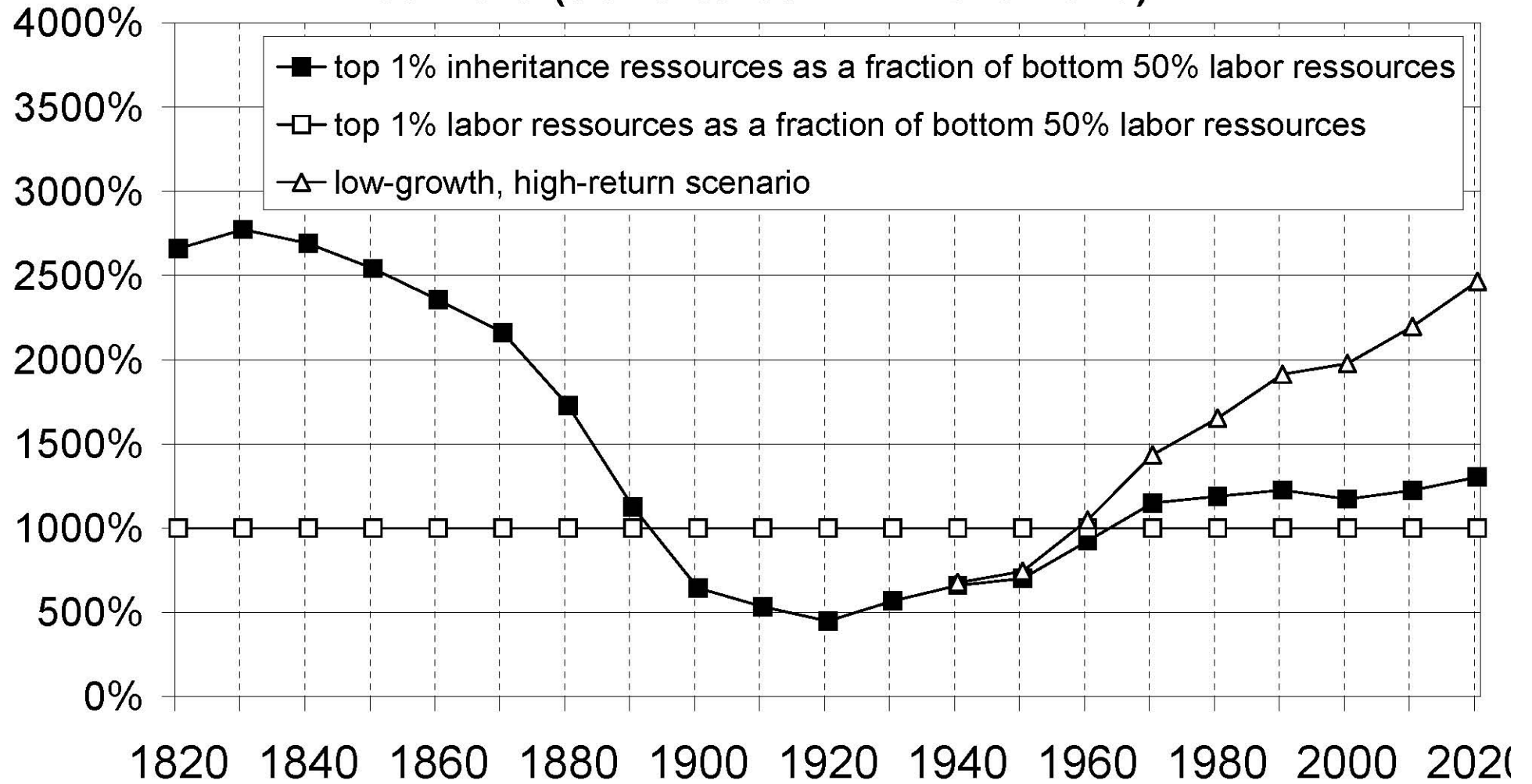
**Figure 12: Top 50% successors vs top 50% labor income earners (cohorts born in 1820-2020)**



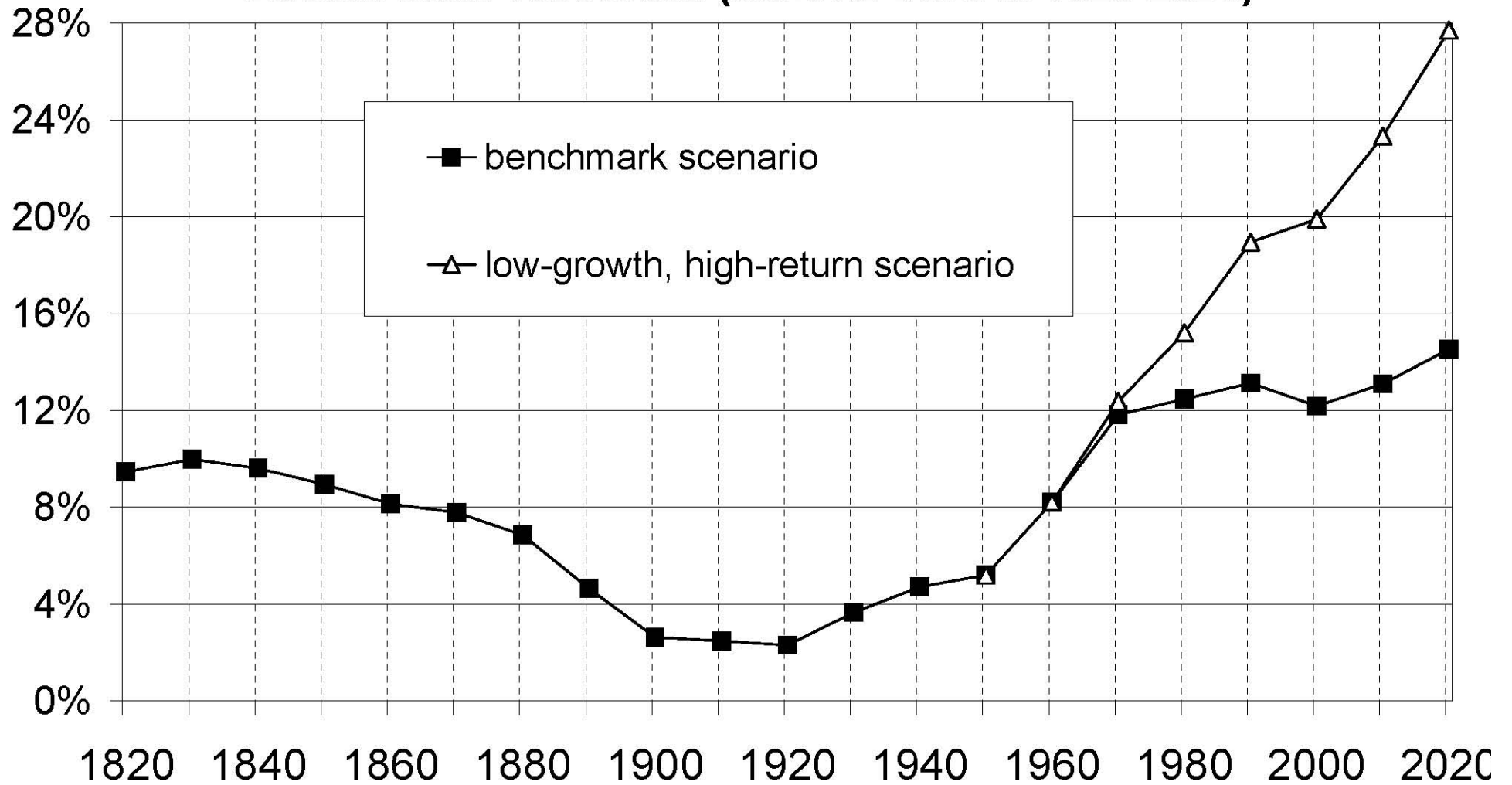
**Figure 13: Top 10% successors vs top 10% labor income earners (cohorts born in 1820-2020)**



**Figure 14: Top 1% successors vs top 1% labor income earners (cohorts born in 1820-2020)**



**Figure 15: Cohort fraction inheriting more than bottom 50% lifetime labor resources (cohorts born in 1820-2020)**

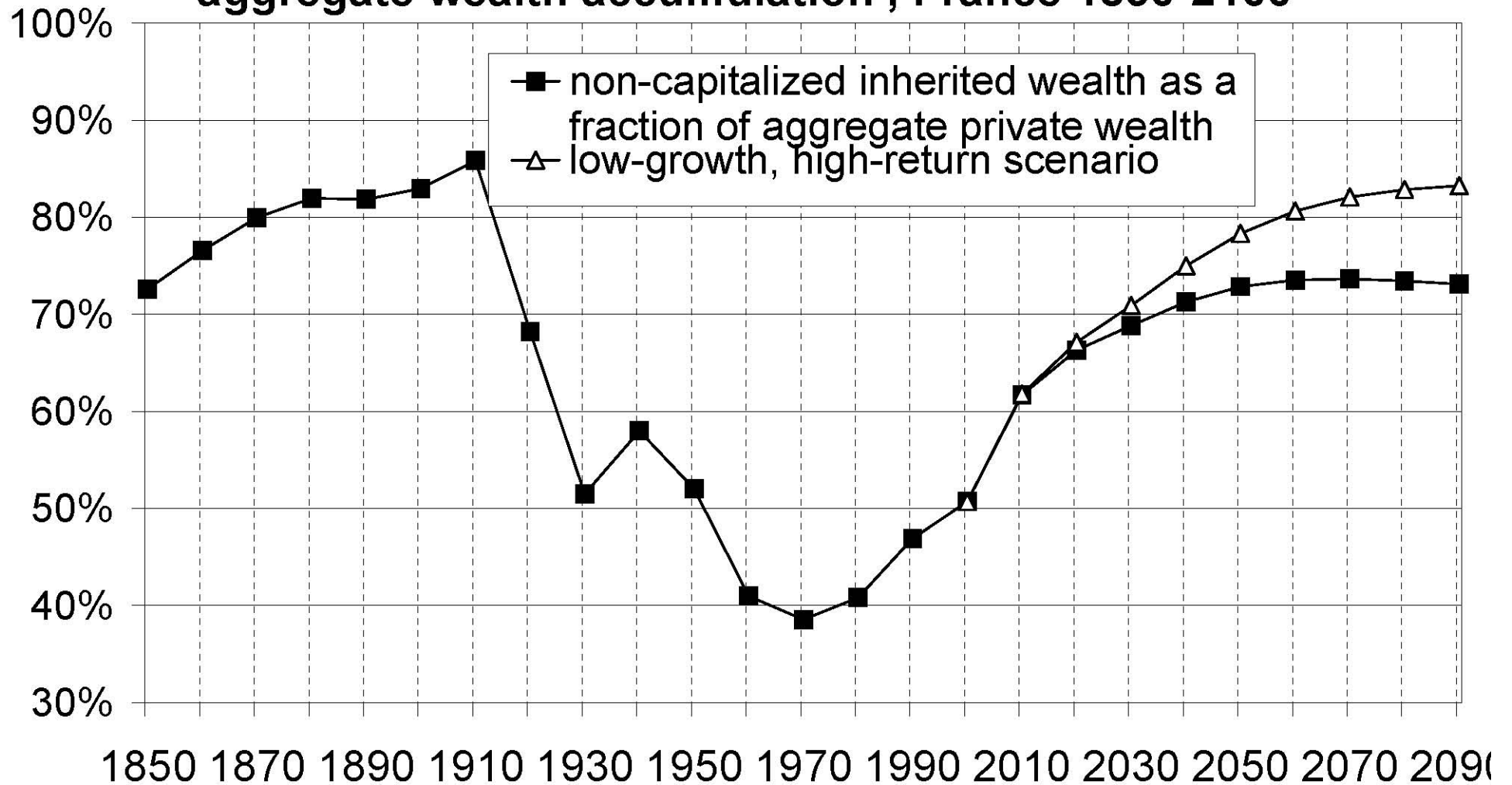




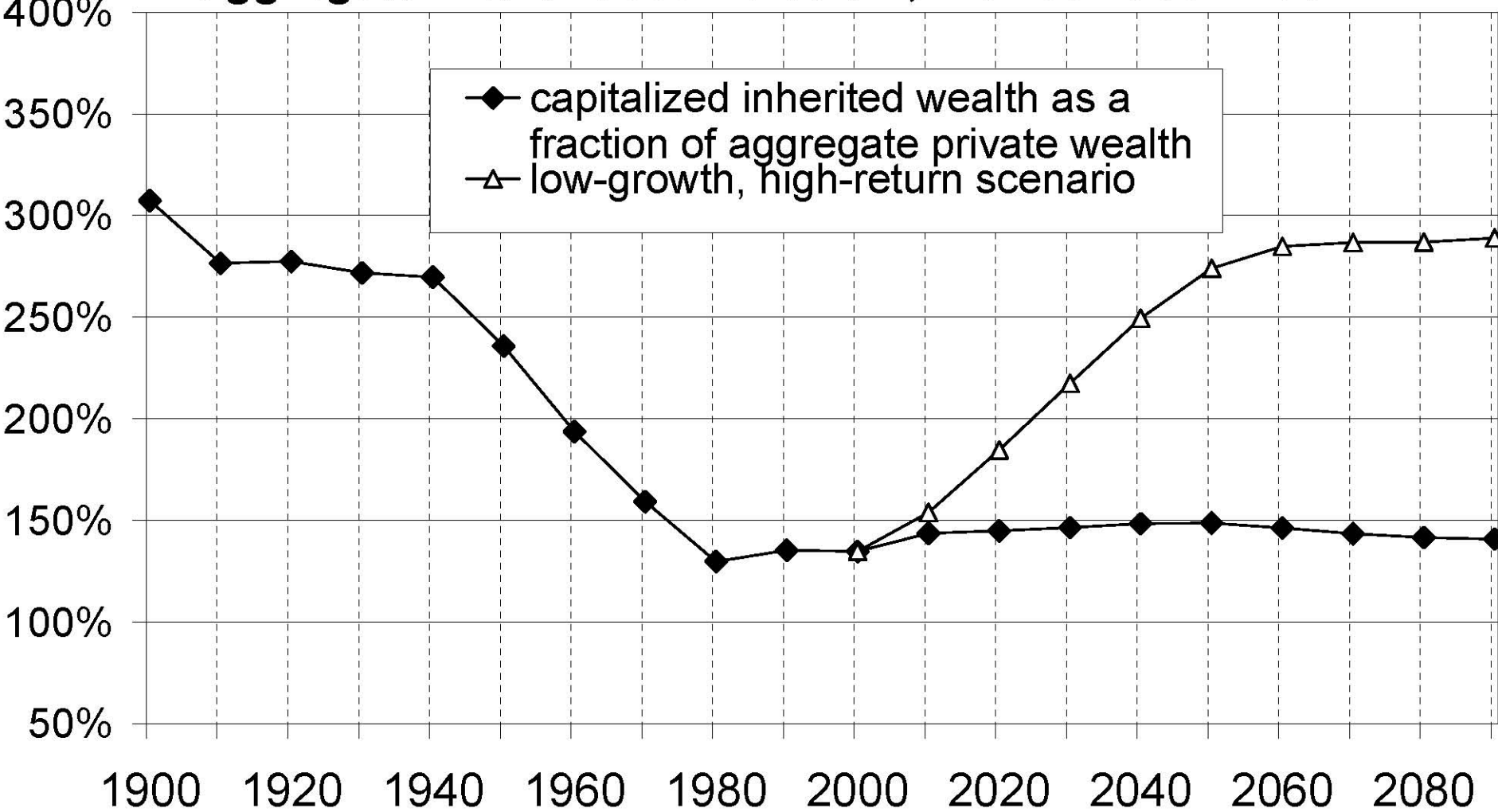
# Application to the share of inheritance in total wealth

- Modigliani AER 1986, JEP 1988: inheritance = 20% of total U.S. wealth
- Kotlikoff-Summers JPE 1981, JEP 1988: inheritance = 80% of total U.S. wealth
- Three problems: - Bad data
- **We do not live in a stationary world: life-cycle wealth was much more important in the 1950s-1970s than it is today**
- **We do not live in a representative-agent world → new definition of inheritance share**

**Figure 18: The share of non-capitalized inheritance in aggregate wealth accumulation , France 1850-2100**



**Figure 19: The share of capitalized inheritance in aggregate wealth accumulation , France 1900-2100**



# What have we learned?

- Capital accumulation takes time; one should not look at past 10 or 20 yrs and believe this is steady-state; life cycle theorists were too much influenced by what they saw in the 1950s-1970s...
- Inheritance is likely to be a big issue in the 21st century
- Modern economic growth did not kill inheritance; the rise of human capital simply did not happen;  $g > 0$  but small not very different from  $g = 0$

- **A lot depends on  $r$  vs  $g+n$ :**
  - China/India: inheritance doesn't matter
  - US: inheritance smaller than in Europe
  - Italy, Spain, Germany ( $n < 0$ ): U-shaped pattern probably even bigger than France
  - world, very long run:  $g+n=0\%$ : inheritance and past wealth will play a dominant role; back to 19th century intuitions
- But no normative model... difficult conceptual issues before we have good optimal  $k$  tax theory (endogenous  $r$ )
  - see Piketty-Saez, in progress...

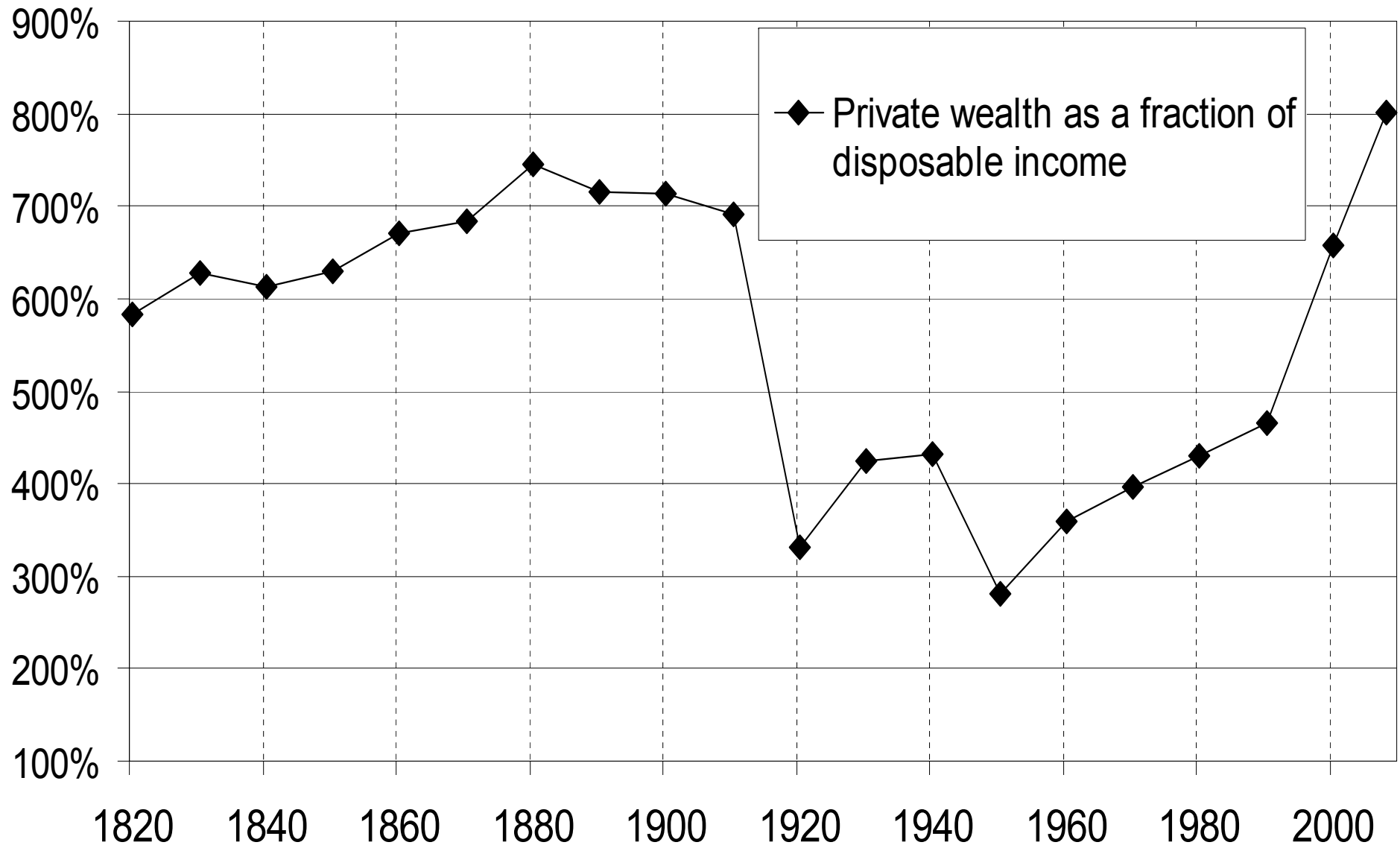
**Table 1: Accumulation of private wealth in France, 1820-2009**

	Real growth rate of national income $g$	Real growth rate of private wealth $g_w$	Savings-induced wealth growth rate $g_{ws} = s/\beta$	Capital-gains-induced wealth growth rate $q$	<i>Memo:</i> <i>Consumer price inflation</i> $p$
1820-2009	1.8%	1.8%	2.1%	-0.3%	4.4%
1820-1913	1.0%	1.3%	1.4%	-0.1%	0.5%
1913-2009	2.6%	2.4%	2.9%	-0.4%	8.3%
1913-1949	1.3%	-1.7%	0.9%	-2.6%	13.9%
1949-1979	5.2%	6.2%	5.4%	0.8%	6.4%
1979-2009	1.7%	3.8%	2.8%	1.0%	3.6%

**Table 2: Rates of return vs growth rates in France, 1820-2009**

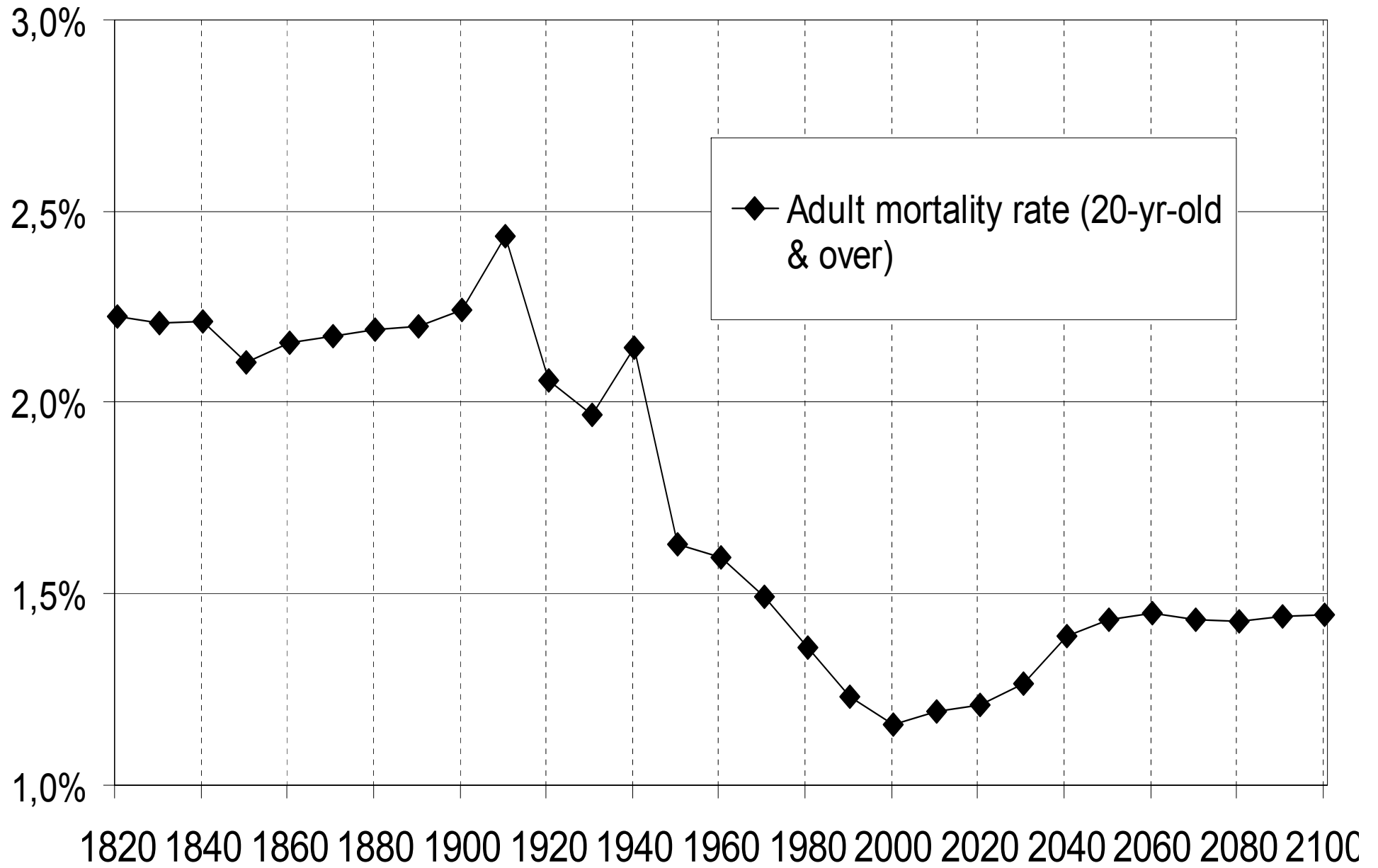
	Growth rate of national income $g$	Rate of return on private wealth $r = \alpha/\beta$	Capital tax rate $T_K$	After-tax rate of return $r_d = (1-T_K)\alpha/\beta$	Real rate of capital gains $q$	Rate of capital destruct. (wars) $d$	After-tax real rate of return (incl. k gains & losses) $r_d = (1-T_K)\alpha/\beta + q + d$
1820-2009	<b>1.8%</b>	<b>6.8%</b>	19%	<b>5.4%</b>	-0.1%	-0.3%	<b>5.0%</b>
1820-1913	<b>1.0%</b>	<b>5.9%</b>	8%	<b>5.4%</b>	-0.1%	0.0%	<b>5.3%</b>
1913-2009	<b>2.6%</b>	<b>7.8%</b>	31%	<b>5.4%</b>	-0.1%	-0.7%	<b>4.6%</b>
1913-1949	<b>1.3%</b>	<b>7.9%</b>	21%	<b>6.4%</b>	-2.6%	-2.0%	<b>1.8%</b>
1949-1979	<b>5.2%</b>	<b>9.0%</b>	34%	<b>6.0%</b>	0.8%	0.0%	<b>6.8%</b>
1979-2009	<b>1.7%</b>	<b>6.9%</b>	39%	<b>4.3%</b>	1.0%	0.0%	<b>5.3%</b>

**Figure 5: Wealth/disposable income ratio France 1820-2008**

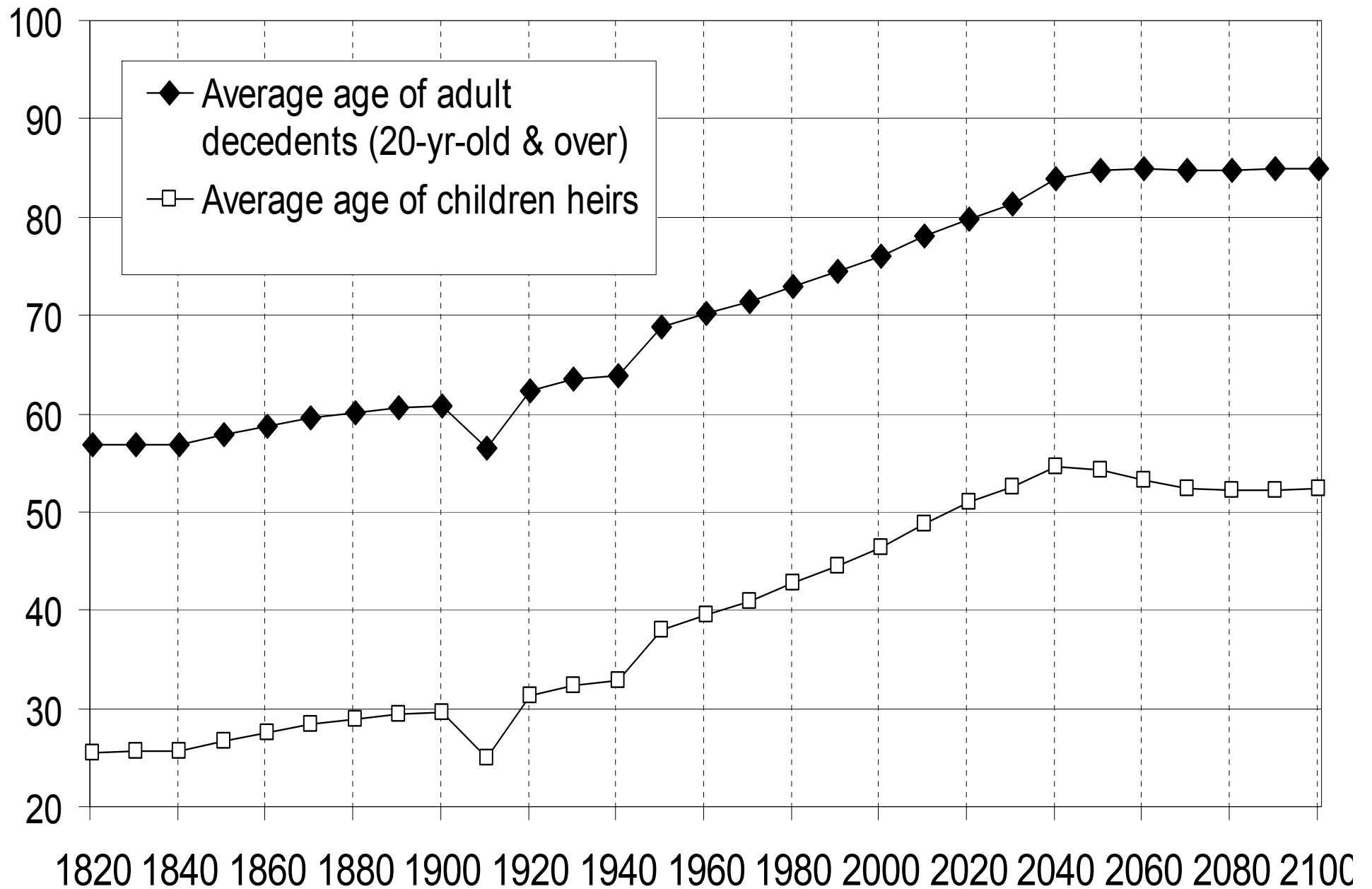




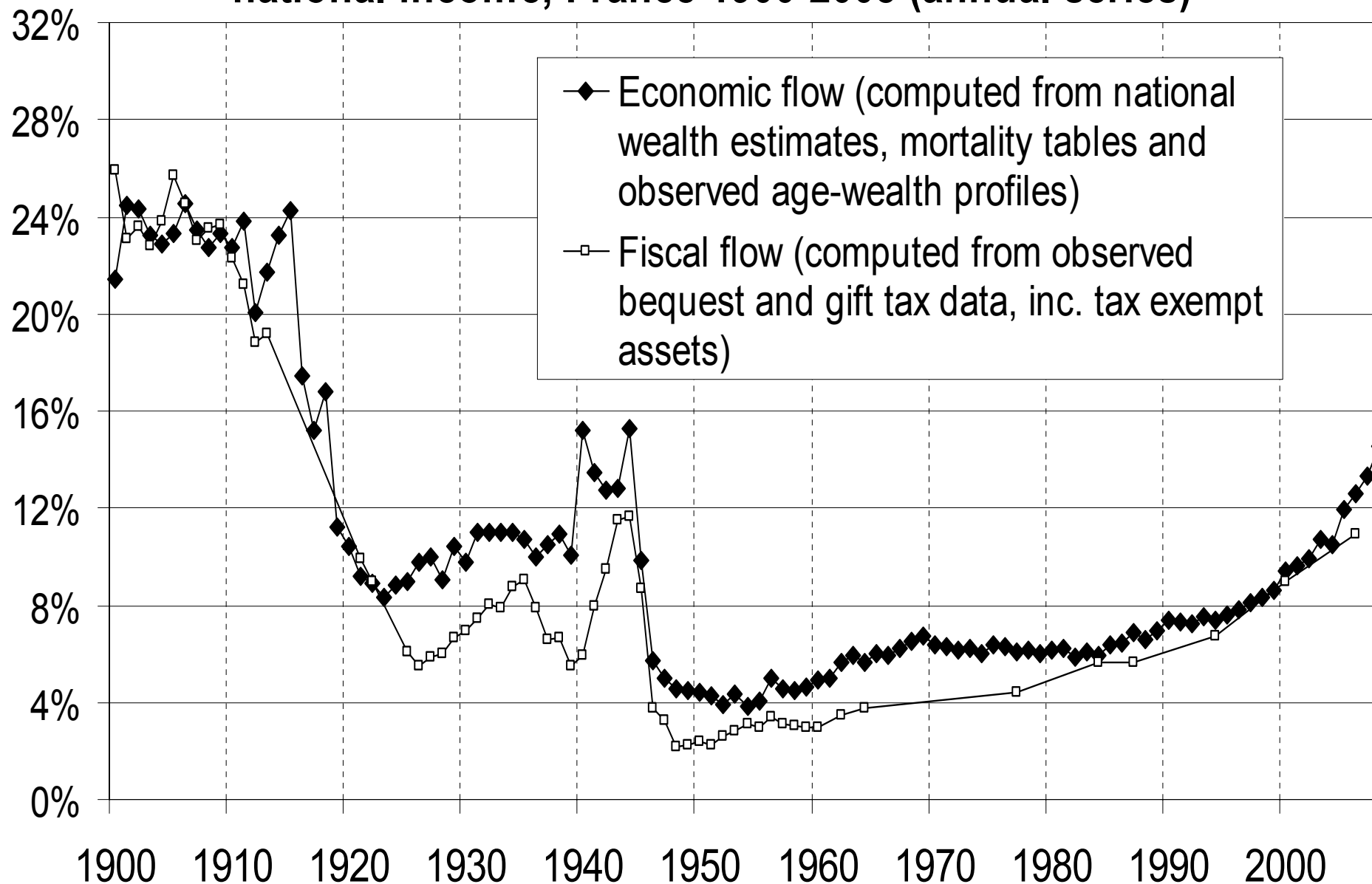
**Figure 6: Mortality rate in France, 1820-2100**



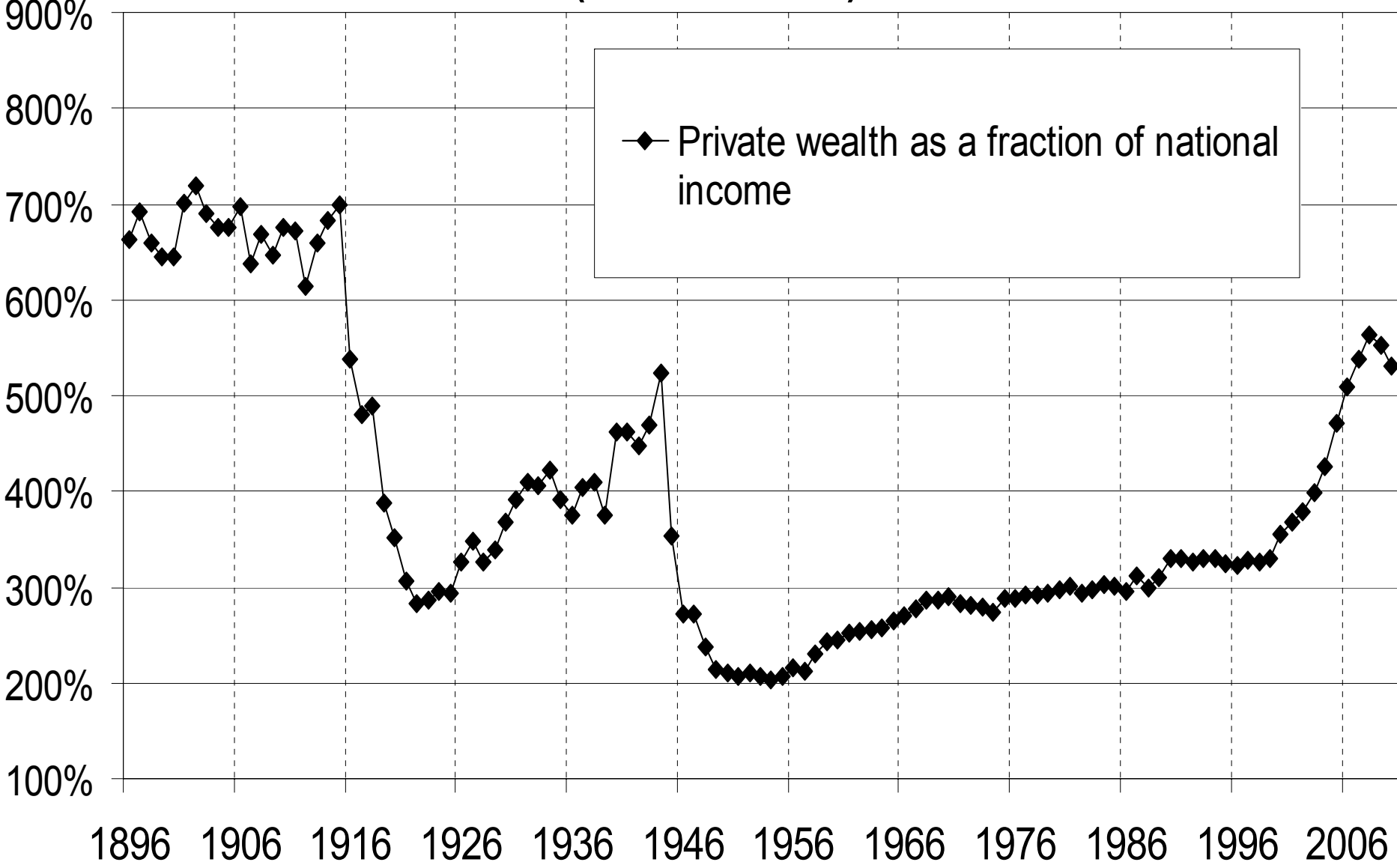
**Figure 7: Age of decedents & heirs in France, 1820-2100**



**Figure A1: Annual inheritance flow as a fraction of national income, France 1900-2008 (annual series)**



**Figure A2: Wealth-income ratio in France 1896-2009**  
**(annual series)**



**Figure A3: Wealth-disposable income ratio in France 1896-2009 (annual series)**

